# **Atomic Commitment Across Blockchains**

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# ABSTRACT

The recent adoption of blockchain technologies and open permissionless networks suggest the importance of peer-topeer atomic cross-chain transaction protocols. Users should be able to atomically exchange tokens and assets without depending on centralized intermediaries such as exchanges. Recent peer-to-peer atomic cross-chain swap protocols use hashlocks and timelocks to ensure that participants comply to the protocol. However, an expired timelock could lead to a violation of the all-or-nothing atomicity property. An honest participant who fails to execute a smart contract on time due to a crash failure, denial of service attacks or even network delays might end up losing assets. Although a crashed participant is the only participant who ends up worse off, current proposals are unsuitable for atomic crosschain transactions in asynchronous environments where

crash failures and network delays are the norm. In this paper, we present  $AC^3WN$ , the first decentralized all-ornothing *atomic* cross-chain commitment protocol. The redeem and refund events of the smart contracts that exchange assets are modeled as conflicting events. An open permissionless network of witnesses is used to guarantee that conflicting events could never simultaneously occur and either all smart contracts in an atomic cross-chain transaction are redeemed or all of them are refunded.

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# **1** Introduction

The wide adoption of permissionless open blockchain networks by both industry (e.g., Bitcoin [22], Ethereum [28], etc) and academia (e.g., Bzycoin [18], Elastico [19], BitcoinNG [11], Algorand [21], etc.) suggests the importance of

*Proceedings of the VLDB Endowment*, Vol. 13, No. 9 ISSN 2150-8097. DOI: https://doi.org/10.14778/3397230.3397231 developing protocols and infrastructures that support peerto-peer atomic cross-chain transactions. Users, who usually do not trust each other, should be able to directly exchange their tokens and assets that are stored on different blockchains (e.g., Bitcoin and Ethereum) without depending on trusted third party intermediaries. Decentralized permissionless [20] blockchain ecosystems require infrastructure enablers and protocols that allow users to atomically exchange tokens without giving up trust-free decentralization, the main reasons behind using permissionless blockchains. We motivate the problem of atomic cross-chain transactions and discuss the current available solutions and their limitations through the following example.

Suppose Alice owns X bitcoins and she wants to exchange them for Y ethers. Luckily, Bob owns ether and he is willing to exchange his Y ethers for X bitcoins. to atomically exchange assets that reside in different blockchains. In addition, both Alice and Bob do not trust each other and in many scenarios, they might not be co-located to do this atomic exchange in person. Current infrastructures do not support these direct peer-to-peer transactions. Instead, both Alice and Bob need to **independently** exchange their tokens through a trusted centralized exchange, Trent (e.g., Coinbase [3] and Robinhood [4]) either through fiat currency or directly. Using Fiat, both Alice and Bob first exchange their tokens with Trent for a fiat currency (e.g., USD) and then use the earned fiat currency to buy the other token also from Trent or from another trusted exchange. Alternatively, some exchanges (e.g., Coinbase) allow their customers to directly exchange tokens (e.g., ether for bitcoin or bitcoin for ether) without going through fiat currencies.

These solutions have many drawbacks that make them unacceptable solutions for peer-to-peer atomic cross-chain transactions. First, they require both Alice and Bob to trust Trent. This centralized trust requirement risks to derail the whole idea of blockchain's trust-free decentralization [22]. Second, they require Trent to trade in all involved resources (e.g., bitcoin and ether). This requirement is unrealistic especially if Alice and Bob want to exchange commodity resources (e.g., transfer a car ownership for bitcoin assuming car titles are stored in a blockchain [16]). Third, these solutions do not ensure the atomic execution of the transaction among the involved participants. Alice might trade her bitcoin directly for ether or through a fiat currency while Bob has no obligation to execute his part of the swap. Finally, these solutions significantly increase the number of required transactions to achieve the intended cross-chain transaction, and hence drastically increases the imposed fees. One cross-

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chain transaction between Alice and Bob results in either four transactions (two between Alice and Trent and two between Bob and Trent) if fiat is used or at best two transactions (one between Alice and Trent and one between Bob and Trent) if assets are directly swapped.

An Atomic Cross-Chain Transaction,  $AC^2T$ , is a distributed transaction that spans multiple blockchains. This distributed transaction consists of sub-transactions and each sub-transaction is executed on a blockchain. An Atomic Cross-Chain Commitment,  $AC^3$ , protocol is required to execute AC<sup>2</sup>Ts. This protocol is a variation of traditional distributed atomic commitment protocols (e.g., 2PC [8, 14]). This protocol should guarantee both *atomicity* and *commitment* of  $AC^2Ts$ . Atomicity ensures the all-or-nothing property where either all sub-transactions take place or none of them do. Commitment guarantees that any changes caused by a cross-chain transaction must eventually take place if the transaction is decided to commit. Unlike in 2PC and other traditional distributed atomic commitment protocols, atomic cross-chain commitment protocols are also trust-free and therefore must **tolerate** maliciousness [16].

A two-party atomic cross-chain commitment protocol was originally proposed by Nolan [1,23] and generalized by Herlihy [16] to process multi-party atomic cross-chain transactions, or swaps. Both Nolan's protocol and its generalization by Herlihy use smart contracts, hashlocks, and timelocks to execute atomic cross-chain transactions. A smart contract is a self executing contract (or a program) that gets executed in a blockchain once all the terms of the contract are satisfied. A hashlock is a cryptographic one-way hash function h = H(s) that locks assets in a smart contract until a hash secret s is provided. A timelock is a time bounded lock that triggers the execution of a smart contract function after a pre-specified time period.

The atomic swap between Alice and Bob, explained in the earlier example, is executed using Nolan's protocol as follows. Let a participant be the leader of the swap, say Alice. Alice creates a secret s, only known to Alice, and a hashlock h = H(s). Alice uses h to lock X bitcoins in a smart contract  $SC_1$  and publishes  $SC_1$  in the Bitcoin network.  $SC_1$  transfers X bitcoins to Bob if Bob provides the secret s to  $SC_1$  where h = H(s). In addition,  $SC_1$  is locked with a timelock  $t_1$  that refunds the X bitcoins to Alice if Bob fails to provide s to  $SC_1$  before  $t_1$  expires. As  $SC_1$  is published in the Bitcoin network and made public to everyone, Bob can verify that  $SC_1$  indeed transfers X bitcoins to his public address if he provides s to  $SC_1$ . In addition, Bob learns h from  $SC_1$ . Using h, Bob publishes a smart contract  $SC_2$  in the Ethereum network that locks Y ethers in  $SC_2$  using h.  $SC_2$  transfers Y ethers to Alice if Alice provides the secret s to  $SC_2$ . In addition,  $SC_2$  is locked with a timelock  $t_2 < t_1$ that refunds the Y ethers to Bob if Alice fails to provide sto  $SC_2$  before  $t_2$  expires.

Now, if Alice wants to redeem her Y ethers from  $SC_2$ , Alice must reveal s to  $SC_2$  before  $t_2$  expires. Once s is provided to  $SC_2$ , Alice redeems the Y ethers and s gets revealed to Bob. Now, Bob can use s to redeem his X bitcoins from  $SC_1$  before  $t_1$  expires. Notice that  $t_1 > t_2$  is a necessary condition to ensure that Bob has enough time to redeem his X bitcoins from  $SC_1$  after Alice provides s to  $SC_2$  and before  $t_1$  expires. If Bob provides s to  $SC_1$  before  $t_1$  expires, Bob successfully redeems his X bitcoins and the atomic swap is marked completed. The case against the current proposals: If Bob fails to provide s to  $SC_1$  before  $t_1$  expires due to a crash failure, a network partitioning, or a network denial of service at Bob's site, Bob loses his X bitcoins and  $SC_1$  refunds the X bitcoins to Alice. This violation of the atomicity property of the protocol penalizes Bob for a failure that happens out of his control. Although a crashed participant is the only participant who ends up being worse off (Bob in this example), this protocol does not guarantee the atomicity of  $AC^2Ts$  in asynchronous environments where crash failures, network partitioning, and message delays are the norm.

Another important drawback in Nolan's and Herlihy's protocols is the requirement to sequentially publish the smart contracts in an atomic swap before the leader (Alice in our example) reveals the secret *s*. This requirement is necessary to ensure that the publishing events of all the smart contracts in the atomic swap *happen before* the redemption of any of the smart contracts. This causality requirement ensures that any malicious participant who declines to publish their payment smart contract cannot take advantage of the protocol. However, the sequential publishing of smart contracts, especially in atomic swaps that include many participants, proportionally increases the latency of the swap to the number of sequentially published contracts.

In this paper, we propose  $AC^3WN$ , the first decentralized all-or-nothing Atomic Cross-Chain Commitment protocol that uses an open Witness Network to coordinate  $AC^2Ts$ . The redemption and the refund events of smart contracts in  $AC^2T$  are modeled as conflicting events. A decentralized open network of witnesses is used to guarantee that conflicting events must never simultaneously take place and either all smart contracts in an  $AC^2T$  are redeemed or all of them are refunded. Unlike in Nolan's and Herlihy's protocols,  $AC^3WN$  allows all participants to concurrently publish their contracts in a swap resulting in a drastic decrease in the latency of atomic swaps. Our contributions are summarized as follows:

- We present AC<sup>3</sup>WN, the first all-or-nothing atomic cross-chain commitment protocol. AC<sup>3</sup>WN is decentralized and its correctness does not depend on any trusted centralized intermediary.
- We prove the correctness of AC<sup>3</sup>WN showing that AC<sup>3</sup>WN achieves both atomicity and commitment of AC<sup>2</sup>Ts.
- Finally, we analytically evaluate AC<sup>3</sup>WN in comparison to Herlihy's [16] protocol. Unlike in Herlihy's protocol where the latency of an atomic swap proportionally increases as the number of the sequentially published smart contracts in the atomic swap increases, our analysis shows that the latency of an atomic swap in AC<sup>3</sup>WN is constant irrespective of the number of smart contracts involved.

The rest of the paper is organized as follows. In Section 2, we discuss the open blockchain data and transactional models. Section 3 explains the cross-chain distributed transaction model and Section 4 presents  $AC^3WN$ , our atomic cross-chain commitment protocol. The  $AC^3WN$  protocol is analyzed in Section 5. The protocol is evaluated in Section 6 and the paper is concluded in Section 7.

# 2 Open Blockchain Models

## 2.1 Architecture Overview

An open permissionless blockchain system [20] (e.g., Bitcoin and Ethereum) typically consists of two layers: a storage layer and an application layer. The storage layer comprises a decentralized distributed ledger managed by an open network of computing nodes. A blockchain system is permissionless if computing nodes can join or leave the network of its storage layer at any moment without obtaining permission from a centralized authority. Each computing node, also called a *miner*, maintains a copy of the ledger. The ledger is a tamper-proof chain of blocks, hence named blockchain. Each block contains a set of valid transactions that transfer assets among end-users. The application layer comprises end-users who communicate with the storage layer via message passing through a client library. Endusers have identities, defined by their public keys, and signatures, generated using their private keys. Digital signatures are the end-users' way to generate transactions as explained later in Section 2.3. End-users submit their transactions to the storage layer through a client library. Transactions are used to transfer assets from one identity to another. Endusers multicast their transaction messages to mining nodes in the storage layer.

A mining node validates the transactions it receives and valid transactions are added to the current block of a mining node. Miners run a consensus protocol through mining to agree on the next block to be added to the chain. A miner who mines a block gets the right to add the mined block to the chain and multicasts it to other miners. To make progress, miners accept the first received mined block after verifying it and start mining the next block<sup>1</sup>. Sections 2.2 and 2.3 explain the data model and the transactional model of open blockchain systems respectively.

### 2.2 Data Model

The storage layer stores the ownership information of assets in the system in the blockchain. The ownership is determined through identities and identities are typically implemented using public keys. In addition, the blockchain stores transactions that transfer the ownership of an asset from one identity to another. Therefore, an asset can be tracked from its registration in the blockchain, the first owner, to its last owner in the blockchain. For example, the Bitcoin blockchain stores the information of the most recent owner of every bitcoin in the Bitcoin blockchain. A bitcoin that is linked to Alice's public key is owned by Alice. Also, new bitcoins are generated and registered in the Bitcoin blockchain through mining. Asset ownership transfers are implemented through transactions.

#### 2.3 Transaction Model

A transaction is a digital signature that transfers the ownership of assets from one identity to another. End-users, in the application layer, use their private keys [26] to digitally sign assets linked to their identity to transfer these assets to other identities, identified by their public keys. These digital signatures are submitted to the storage layer via message passing through a client library. It is the responsibility of the miners to validate that end-users can transact only on their own assets. If an end-user digitally signs an asset that is not owned by this end-user, the resulting transaction is not valid and hence rejected by the miners. In addition, miners validate that an asset cannot be spent twice and hence prevent double spending of assets.

Another way to perform transactions in blockchain systems is through smart contracts. A smart contract is a program written in some scripting language (e.g., Solidity for Ethereum smart contracts [5]) that allows general program executions by a blockchain's mining nodes. Endusers publish a smart contract in a blockchain through a deployment message, msq, that is sent to the mining nodes in the storage layer. A deployment message includes the smart contract code in addition to some implicit parameters that are accessible to the smart contract code once the smart contract is deployed. These parameters include the sender's public key, accessed through msg.sender, and an optional asset value, accessed through msg.val. This optional asset value allows end-users to send some of their blockchain assets to a deployed smart contract. Like transactions, a smart contract is published in a blockchain if it is included in a mined block in this blockchain. We adopt Herlihy's notion of smart contracts as classes in object oriented programming languages [10, 17]. A smart contract has a state, a constructor that is called when a smart contract is first deployed in the blockchain, and a set of functions that could alter the state of the smart contract. The smart contract constructor gets executed once a smart contract is deployed resulting in instantiating a smart contract object in the blockchain. The constructor initializes the smart contract object and uses the implicit parameters sent alongside the smart contract deployment message to initialize the owner of the smart contract and the assets' value sent to this smart contract. Miners verify that the end-user who deploys a smart contract indeed owns these assets. Once assets are sent to a smart contract, the ownership of these assets is moved to the smart contract itself. Smart contract assets can only be transacted on within the smart contract logic until these assets are unlocked from the smart contract as a result of a smart contract function call. To execute a smart contract function, end-users submit their function call accompanied by the function parameters through messages to miners. These messages could include implicit parameters as well (e.g., msq.sender). Miners execute<sup>2</sup> the function on the current state of the contract and record any contract state changes in their current block in the blockchain. Therefore, a smart contract object state might span many blocks after the block where the smart contract is first deployed.

# 3 Atomic Cross-Chain Transaction Model



Figure 1: An atomic cross-chain transaction graph to swap X bitcoins for Y ethers between Alice (A) and Bob (B).

<sup>&</sup>lt;sup>1</sup>Forks and fork resolutions are discussed in later sections.

<sup>&</sup>lt;sup>2</sup>End-users pay to miners a smart contract deployment fee plus a function invocation fee for every function call.

An Atomic Cross-Chain Transaction,  $AC^{2}T$ , is a

distributed transaction to transfer the ownership of assets stored in multiple blockchains among two or more participants. This distributed transaction consists of

sub-transactions and each sub-transaction transfers an asset on some blockchain. An AC<sup>2</sup>T is modeled using a directed graph  $\mathcal{D} = (\mathcal{V}, \mathcal{E})$  [16] where  $\mathcal{V}$  is the set of vertexes and  $\mathcal{E}$  is the set of edges in  $\mathcal{D}$ .  $\mathcal{V}$  represents the participants in AC<sup>2</sup>T and  $\mathcal{E}$  represents the sub-transactions in AC<sup>2</sup>T. A directed edge  $e = (u, v) \in \mathcal{E}$  represents a sub-transaction that transfers an asset *e.a* from a source participant  $u \in \mathcal{V}$ to a recipient participant  $v \in \mathcal{V}$  in some blockchain *e.BC*. Figure 1 shows an example of an AC<sup>2</sup>T graph between Alice (A) and Bob (B). As shown, the edge (A, B) represents the sub-transaction  $AC^2T_1$  that transfers X bitcoins from A to B while the edge (B, A) represents the sub-transaction  $AC^2T_2$  that transfers Y ethers from B to A.

An atomic cross-chain commitment protocol is required in order to correctly execute an  $AC^2T$ . This protocol must ensure the atomicity and the commitment of all sub-transactions in  $AC^2T$  as follows.

- Atomicity: either all or none of the asset transfers of all sub-transactions in the AC<sup>2</sup>T take place.
- Commitment: once the atomic cross-chain commitment protocol decides the commitment of an AC<sup>2</sup>T, asset transfers of all sub-transactions in this AC<sup>2</sup>T must eventually take place.

An atomic cross-chain commitment protocol is a variation of the two phase commit protocol (2PC) [8,14]. Therefore, we use the analogy of 2PC to explain an abstraction of the atomic cross-chain commitment protocol. In 2PC, a distributed transaction spans multiple data partitions and each partition is responsible for executing a sub-transaction. A coordinator sends a vote request to all involved data partitions. Upon receiving a vote request, a data partition votes back yes only if it succeeds in executing all the operations of its sub-transaction on the involved data objects. Otherwise, a data partition votes no to the coordinator. A coordinator decides to commit a distributed transaction if all involved data partitions vote yes, otherwise it decides to abort the distributed transaction. If a commit decision is reached, all data partitions commit their sub-transactions. However, if an abort is decided, all data partitions must abort their sub-transactions. 2PC assumes that the coordinator and the data partitions are trusted. The main challenge in blockchain systems is how to design a trust-free variation of 2PC where participants do not trust each other and a protocol cannot depend on a centralized trusted coordinator.

Consider an AC<sup>2</sup>T  $\mathcal{A}$ . An atomic cross-chain commitment protocol requires that for every edge  $e = (u, v) \in \mathcal{E}$ , the source participant u locks an asset e.a in Blockchain e.BC. This asset locking is necessary to temporarily prevent the participant u from spending e.a through other transactions in e.BC. If every source participant u locks e.a in e.BC, the atomic cross-chain commitment protocol can decide to commit  $\mathcal{A}$ . Once the protocol decides to commit  $\mathcal{A}$ , every recipient participant v should be able to *redeem* the asset e.a. However, if the protocol decides to abort  $\mathcal{A}$  because some participants do not comply with the protocol or a participant requests the transaction to abort, every source participant u should be able to get a refund of their locked assets e.a.

In blockchain systems, smart contracts are used to implement this logic. For each edge e = (u, v), participant udeploys a smart contract  $SC_e$  in Blockchain e.BC to lock an asset e.a owned by u in  $SC_e$ .  $SC_e$  ascertains to conditionally transfer e.a to v if a commitment decision is reached, otherwise e.a is refunded to u. A smart contract  $SC_e$  exists in one of three states: published (P), redeemed (RD), or refunded (RF). A smart contract  $SC_e$  is published if it gets deployed to e.BC by u. Publishing the smart contract  $SC_e$ serves two important goals towards the atomic execution of  $\mathcal{A}$ . First, it represents a *yes* vote on the sub-transaction corresponding to the edge e. Second, it locks the asset e.ain blockchain e.BC. A smart contract  $SC_e$  is redeemed if participant v successfully redeems the asset e.a from  $SC_e$ . Finally, a smart contract  $SC_e$  is refunded if the asset e.a is refunded to participant u.

Now, if for every edge  $e = (u, v) \in \mathcal{E}$ , the participant u publishes a smart contract  $SC_e$  in e.BC, it means that all participants vote yes on  $\mathcal{A}$ , lock their involved assets in  $\mathcal{A}$ , and hence  $\mathcal{A}$  can commit. However, if some participants decline to publish their smart contracts,  $\mathcal{A}$  has to abort. The commitment of  $\mathcal{A}$  requires the redemption of **every** smart contract  $SC_e$  in  $\mathcal{A}$ . On the other hand, if  $\mathcal{A}$  aborts, this requires the refund of **every** smart contract  $SC_e$  in  $\mathcal{A}$ .

To implement conditional smart contract redemption and refund, a cryptographic commitment scheme primitive based on [12] is used. A commitment scheme allows a user to commit to some chosen value without revealing this value. Once this hidden value is revealed, other users can verify that the revealed value is indeed the one that is used in the commitment. A hashlock is an example of a commitment scheme. A hashlock is a cryptographic one-way hash function h = H(s) that is used to conditionally lock assets in a smart contract using h, the lock, until a hash secret s, the key, is revealed. Once s is revealed, everyone can verify that lock h equals H(s) and hence unlocks the assets locked in the smart contract.

An atomic cross-chain commitment protocol should ensure that smart contracts in  $\mathcal{A}$  are either all redeemed or all refunded. For this, a protocol uses two mutually exclusive commitment scheme instances: a redemption commitment scheme and a refund commitment scheme. All smart contracts in  $\mathcal{A}$  commit their redemption action to the redemption commitment scheme instance and their refund action to the refund commitment scheme instance. If the protocol decides to commit  $\mathcal{A}$ , the protocol must publish the redemption commitment scheme secret. This allows all participants in  $\mathcal{A}$  to redeem their assets. However, if the protocol reaches an abort decision, the protocol must publish the refund commitment scheme secret. This allows participants in  $\mathcal{A}$  to refund the locked assets in every published smart contract. A protocol must ensure that once the secret of one commitment scheme instance is revealed, the secret of the other instance cannot be revealed. This guarantees the *atomic* execution of  $\mathcal{A}$ .

Algorithm 1 illustrates a smart contract template that can be used in implementing an atomic cross-chain commitment protocol. Each smart contract has a sender s and recipient r (Line 2), an asset a (Line 3) to be transferred from s to r through the contract, a state (Line 4), and a redemption and refund commitment scheme instances rd and rf (Lines 5 and 6). A smart contract is published in a blockchain through a deployment message. When published, its constructor (Line 7) is executed to initialize the contract. The deployment message of a smart contract typically includes some implicit parameters like the sender's address (msg.sender, Line 8) and the asset value (msg.val, Line 9) to be locked in the contract. The constructor initializes the addresses, the asset value, the refund and redemption commitment schemes, and sets the contract state to P (Line 11).

 Algorithm 1 An atomic swap smart contract template

 abstract class AtomicSwapSC {

- 1: enum State {Published (P), Redeemed (RD), Refunded (RF)}
- 2: Address s, r // Sender and recipient public keys.
- 3: Asset a
- 4: State state
- 5: CS rd // Redemption commitment scheme
- 6: CS rf // Refund commitment scheme
- 7: procedure CONSTRUCTOR(Address r, CS rd, CS rf)
- 8: this.s = msg.sender, this.r = r
- 9: this.a = msg.val

```
10: this.rd = rd, this.rf = rf
```

- 11: state = P
- 12: end procedure

```
13: procedure REDEEM(Evidence evd_{rd})
       requires(state == P and IsRedeemable(evd_{rd}))
14:
       transfer a to r, state = RD
15:
16:
    end procedure
17:
    procedure REFUND(Evidence evd_{rf})
18:
       requires(state == P and IsRefundable(evd_{rf}))
19:
       transfer a to s, state = RF
20: end procedure
21: procedure IsRedeemable(Evidence evd_{rd})
22:
       return verify(rd, evd_{rd})
23: end procedure
24:
   procedure IsRefUNDABLE(Evidence evd_{rf})
25:
       return verify(rf, evd_{rf})
26: end procedure
```

}

In addition, each smart contract has a redeem function (Line 13) and a refund function (Line 17). A redeem function takes an evidence parameter. This evidence parameter proves that the decision is to commit  $AC^2T$ . The redeem function requires the smart contract to be in state P and that the provided evidence is a valid redemption commitment scheme secret (Line 14). If all these requirements hold, the asset a is transferred from the contract to the recipient and the contract state is changed to RD. However, if any requirement is violated, the redeem function fails and the smart contract state remains unchanged.

Similarly, the refund function requires the smart contract to be in state P and that the provided evidence is a valid refund commitment scheme secret (Line 18). If all these requirements hold, the asset a is refunded from the contract to the sender and the contract state is changed to RF.

The redeem and the refund functions use *two* helper functions: IsRedeemable (Line 21) and IsRefundable (Line 24). IsRedeemable verifies that the provided evidence is a valid redemption commitment scheme secret and hence the smart contract can be redeemed. Similarly, IsRefundable verifies that the provided evidence is a valid refund commitment scheme secret and hence the smart contract can be refunded.

#### 4 AC<sup>3</sup>: Atomic Cross-Chain Commitment

This section presents AC<sup>3</sup>WN, an Atomic Cross-Chain Commitment  $(AC^3)$  protocol that achieves both **atomicity** and **commitment** of an  $AC^{2}T$ . First, Section 4.1 presents an important building block on how miners of one blockchain validate the publishing of a transaction or a smart contract in another blockchain. Second, we present  $AC^{3}WN$ , an  $AC^{3}$ protocol that uses a permissionless Witness Network to coordinate  $AC^2Ts$  in Section 4.2. Also, Section 4.2 explains how the witness network miners ensure the integrity of a smart contract code deployed in another blockchain. Using a permissionless network of witnesses does not require more trust in the witness network than the required trust in the blockchains used to exchange the assets in an  $AC^{2}T$ . Furthermore, the AC<sup>3</sup>WN protocol overcomes the vulnerability of centralized solutions that are subject to failures and denial of service attacks.

#### 4.1 Cross-Chain Validation

This section explains different techniques for how the miners of one blockchain, the validators, can validate the publication and verify the state of a smart contract deployed in another blockchain, the validated blockchain. A simple but impractical solution is to require all the miners of every blockchain to serve as validators of all other blockchains. A blockchain validator maintains a copy of the validated blockchain and for every newly mined block, a validator validates the mined block and adds it to its local copy of the validated blockchain. If all mining nodes mine one blockchain and validate all other blockchains, mining nodes can consult their local copies of these blockchains to validate the publishing and hence verify the state of any smart contract in any blockchain. If a participant needs the miners of the validator blockchain to validate the publishing of a smart contract in some other validated blockchain, this participant submits evidence that comprises the block id and the transaction id of the smart contract in the validated blockchain to the miners of the validator blockchain. This evidence is easily verified by the mining node of the validator blockchain by consulting their copy of the validated blockchain. However, this full replication of all the blockchains in all the mining nodes is impractical. Not only does it require massive processing power to validate all blockchains, but also it requires significant storage and network capabilities at each mining node.

Alternatively, miners of one blockchain, the validators, can run *light nodes* [9] of other blockchains, the validated blockchains. A light node, as defined in [9], is a node that downloads only block headers of the validated blockchain, verifies the proof of work of these block headers, and downloads only the blockchain branches that are associated with transactions of interest to this node. This solution requires the validators to mine for one blockchain and run light nodes for every validated blockchain. The validators can consult their local light node copy of the validated blockchain to validate the publishing and hence verify the state of a smart contract in the validated blockchain. Although the cost of maintaining a light node is much cheaper than maintaining a blockchain full copy, running a light node for all blockchains does not scale as the number of blockchains increases. The previous two techniques put the onus of validating one blockchain on the miners of another blockchain. In addition, they require changes in the current infrastructure by requiring the miners of one blockchain to either maintain a full copy or a light node of other blockchains.



Figure 2: How miners of one blockchain could validate transactions in another blockchain.

Our proposal: Another way to allow miners of one blockchain, the validators, to validate the publication and verify the state of a smart contract in another blockchain, the validated, is to push the validation logic into the code of a smart contract in the validator blockchain. A smart contract in the validator blockchain is deployed and stores the header of a *stable block* in the validated blockchain. A stable block is a block at depth d from the current head of the validated blockchain such that the probability of forking the blockchain at this block is negligible (e.g., a block at depth  $\geq 6$  in the Bitcoin blockchain [2]). A participant who deploys the smart contract in the validator blockchain stores the block header of a stable block of the validated blockchain as an attribute in the smart contract object in the validator blockchain. When the transaction of the smart contract of interest takes place in a block in the validated blockchain and after this block becomes a stable block, at depth d, a participant can submit evidence of the transaction occurrence in the validated blockchain to the miners of the validator blockchain. This evidence comprises the headers of all the blocks that follow the stored stable block header in the smart contract of the validator blockchain in addition to the block where the transaction of interest took place. The evidence is submitted to the validator smart contract via a function call. This smart contract function validates that the passed headers follow the header of the stable block previously stored in the smart contract object and that the proof of work of each header is valid. In addition, the function verifies that the transaction of interest indeed took place and that the block of this transaction is stable and buried under d blocks in the validated blockchain.

Figure 2 shows an example of a validator blockchain, blockchain<sub>2</sub>, that validates the occurrence of transaction  $TX_1$  in the validated blockchain, blockchain<sub>1</sub>. In this example, there exists a smart contract SC that gets deployed in the current head block of blockchain<sub>2</sub> (labeled by number 2 in Figure 2). SC has an initial state  $S_1$  and stores the header of a stable block, at depth d, in blockchain<sub>1</sub> (labeled by number 1). This header is represented by a red rectangle inside SC. SC's state is altered from  $S_1$  to  $S_2$  if evidence is submitted to miners of blockchain<sub>2</sub> that proves that  $TX_1$  took place in blockchain<sub>1</sub> in some block after the stored stable block header in SC. When  $TX_1$  takes place in blockchain<sub>1</sub> (labeled by number 3) and its block becomes a stable block at depth  $\geq d$  (labeled by number 4), a participant submits the evidence (labeled by number 5) to the miners of blockchain<sub>2</sub> through SC's function call (labeled by number 6). This function takes the evidence as a parameter and verifies that the submitted blocks took place after the stored stable block in SC. This verification ensures that the header of each submitted block includes the hash of the header of the previous block starting from the stored stable block header in SC. In addition, this function verifies the proof of work of each submitted block header. Finally, the function validates that  $TX_1$  took place in some block in the submitted evidence and that this block has already become a stable block. If this verification succeeds, the state of SCis altered from  $S_1$  to  $S_2$ . This technique allows miners of one blockchain to verify transactions and smart contracts in another blockchain without maintaining a copy of this blockchain. In addition, this technique puts the evidence validation responsibility on the developer of the validator smart contract.

#### 4.2 AC<sup>3</sup>WN: Permissionless Witness Network

This section presents  $AC^3WN$ , an  $AC^3$  protocol that uses a *permissionless blockchain network* of witnesses to decide whether an  $AC^2T$  should be committed or aborted. **Miners** of this blockchain are collectively the **witnesses** on  $AC^2Ts$ . The main design challenge of the  $AC^3WN$  protocol is how to use a permissionless network of witnesses to implement the redemption and refund commitment scheme instances used by every smart contract in  $AC^2T$ . In addition, how to ensure that the two instances are *mutually exclusive*.

When a set of participants want to execute an  $AC^2T$ , they deploy a smart contract  $SC_w$  in the witness network where  $SC_w$  is used to coordinate the  $AC^2T$ .  $SC_w$  has a state that determines the state of the  $AC^2T$ .  $SC_w$  exists in one of three states: Published (P), Redeem\_Authorized ( $RD_{auth}$ ), or Refund\_Authorized ( $RF_{auth}$ ). Once  $SC_w$  is deployed,  $SC_w$  is initialized to the state P. If the witness network decides to commit the  $AC^2T$ , the witnesse set  $SC_w$ 's state to  $RD_{auth}$ . However, if the witness network decides to abort the  $AC^2T$ , the witnesses set  $SC_w$ 's state to  $RF_{auth}$ .



Figure 3: Coordinating  $AC^2Ts$  using a permissionless witness network.

Figure 3 shows an AC<sup>2</sup>T that exchanges assets among blockchains, *blockchain*<sub>1</sub>,...,*blockchain*<sub>n</sub> and uses a *witness blockchain* for coordination. Also, it illustrates the AC<sup>3</sup>WN protocol steps. For every AC<sup>2</sup>T, a directed graph  $\mathcal{D} = (\mathcal{V}, \mathcal{E})$ is constructed at some timestamp t and multisigned by all the participants in the set  $\mathcal{V}$  generating a graph multisignature  $ms(\mathcal{D})$  as shown in Equation 1. The timestamp t is important to distinguish between identical  $AC^2Ts$  among the same participants. The order of participant signatures in  $ms(\mathcal{D})$  is not important. Any signature order indicates that all participants in the AC<sup>2</sup>T agree on the graph  $\mathcal{D}$  at some timestamp t.

$$ms(\mathcal{D}) = sig(..., sig(sig((\mathcal{D}, t), p_1), p_2), ..., p_{|\mathcal{V}|})$$
(1)

A participant registers  $ms(\mathcal{D})$  in a smart contract  $SC_w$  in the witness network where  $SC_w$ 's state is initialized to P. The state P indicates that participants of the  $AC^2T$  agreed on  $\mathcal{D}$ . In addition, participants agree to conditionally link the redeem and the refund actions of their smart contracts in the AC<sup>2</sup>T to  $SC_w$ 's states  $RD_{auth}$  and  $RF_{auth}$  respectively. Note that once  $SC_w$  gets deployed in the witness network, the  $SC_w$  object gets a unique address that can be used to reference  $SC_w$  in the redemption and the refund actions of smart contracts that transfer assets among participants. Afterwards, the participants *parallelly* deploy their smart contracts in the blockchains,  $blockchain_1, ..., blockchain_n$ , as shown in Figure 3. After all the participants deploy their smart contracts in the AC<sup>2</sup>T, a participant may submit a state change request to the witness network miners to alter  $SC_w$ 's state from P to  $RD_{auth}$ . This request is accompanied by evidence that all smart contracts in the AC<sup>2</sup>T are deployed and correct. Upon receiving this request, witness network miners verify that  $SC_w$ 's state is P and that participants of the AC<sup>2</sup>T have indeed deployed their smart contracts in the  $AC^2T$  in their corresponding block chains. In addition, miners verify that all these smart contracts are in state P and that the redemption and the refund of these smart contracts are conditioned on  $SC_w$ 's states  $RD_{auth}$ and  $RF_{auth}$  respectively (via  $SC_w$ 's unique address). Finally, witness network miners verify the integrity of each deployed smart contract in AC<sup>2</sup>T through a multi-step process. Since each smart contract is a class and each smart contract deployment is an object instantiation of this class, witness network miners need to verify that the object attributes match their corresponding description in the graph  $\mathcal{D}$  and the object functions have not been tampered with by the smart contract deployer (asset sender). First, witness network miners verify that the attributes of each smart contract such as sender, recipient, and asset amount match the attribute values of the edge corresponding to this smart contract  $\forall e = (u, v) \in \mathcal{D}.\mathcal{E}$ . Then, witness network miners must ensure that the recipient of each transfer smart contract has signed the smart contract functions and that this signature is included in one of the attributes of the smart contract object. This ensures that each recipient has verified the smart contract transfer functions and that the deployer (the sender) of each transfer smart contract cannot tamper with the agreed upon smart contract functions (e.g., redeem and refund functions).

If this verification succeeds for every smart contract in  $AC^2T$ , witness network miners record  $SC_w$  state change to  $RD_{auth}$  in their current block. Once a block that reflects

the state change of  $SC_w$  to  $RD_{auth}$  is mined in the witness network, the commitment of the  $AC^2T$  is decided and participants can use this block as commitment evidence to redeem their assets in the smart contracts of the  $AC^2T$ . The commit decision is illustrated in Figure 3 using the vertical dotted line.

Similarly, if some participants decline to deploy their smart contracts in the  $AC^2T$  or a participant changes her mind before the commitment of the  $AC^2T$ , a participant can submit a state change request to the witness network miners to alter  $SC_w$ 's state from P to  $RF_{auth}$ . The miners of the witness network only verify that  $SC_w$ 's state is P. If this verification succeeds, the miners of the witness network record  $SC_w$ 's state change to  $RF_{auth}$  in their current block. Once a block that reflects the state change of  $SC_w$  to  $RF_{auth}$  is mined in the witness network, the  $AC^{2}T$  is considered aborted and the participants can use this block as evidence of the abort to refund their assets in the deployed smart contracts of the  $AC^{2}T$ . Note that  $SC_{w}$  is programmed to ensure that  $SC_{w}$ 's state can only be changed either from P to  $RD_{auth}$  or from P to  $RF_{auth}$  but no other state transition is allowed. This ensures that  $SC_w$ 's states  $RD_{auth}$  and  $RF_{auth}$  are mutually exclusive. Miners use the cross-chain evidence validation techniques presented in Section 4.1 to validate the deployment of smart contracts in other blockchains.

Algorithm 2 presents the details of  $SC_w$ .  $SC_w$  consists of four functions: Constructor (Line 6), AuthorizeRedeem (Line 12), AuthorizeRefund (Line 16), and VerifyContracts (Line 20). The Constructor initializes  $SC_w$  with the participants' public keys, the multisigned graph of the  $AC^{2}T$ , and the headers of stable blocks in all the involved blockchains in  $AC^2T$ . This information is necessary for the witness network miners to later verify the correctness and the deployment of all smart contracts in the  $AC^{2}T$ . AuthorizeRedeem alters  $SC_w$ 's state from P to  $RD_{auth}$ . To call AuthorizeRedeem, a participant provides evidence of the deployment of all the smart contracts in the  $AC^2T$  (Line 12). AuthorizeRedeem first verifies that  $SC_w$ 's state is currently P. In addition, AuthorizeRedeem verifies that all smart contracts in the AC<sup>2</sup>T are published and correct through a VerifyContracts function call (Line 13). If this verification succeeds,  $SC_w$ 's state is altered to  $RD_{auth}$  (Line 14). On the other hand, AuthorizeRefund verifies only that the state of  $SC_w$ is P (Line 17). If true,  $SC_w$ 's state is altered to  $RF_{auth}$ (Line 18).

VerifyContracts validates that all smart contracts in the  $AC^{2}T$  are published and correct. For every edge  $e = (u, v) \in$  $\mathcal{D}.\mathcal{E}$ , VerifyContracts first verifies the evidence  $evd_e$  corresponding to the edge e (Line 25) as explained in Section 4.1. Then, VerifyContracts finds the matching smart contract  $SC_e$  in  $evd_e$ . Then, VerifyContracts ensures that  $SC_e$  matches its description in the edge e by checking that the smart contract sender is u, the recipient is v, the asset value is e.a, and the redeem and refund commitment schemes are set to  $SC_w$ 's states  $RD_{auth}$  and  $RF_{auth}$  respectively (Lines 27 - 29). Also, VerifyContracts checks the integrity of  $SC_e$ 's functions by checking that the code of  $SC_e$ 's functions matches the signature of the recipient v stored in  $SC_e$  (Line 30). If any verification step fails, VerifyContracts fails and sets the return value to *false* (Line 32). However, if all smart contracts in the provided list are correct, VerifyContracts sets the return value to true (Line 21). VerifyContracts ensures that AuthorizeRedeem cannot be exe-

Algorithm 2 Witness network smart contract as an AC<sup>2</sup>T Coordinator.

class WitnessSmartContract {

- 1: enum State {Published (P), Redeem\_Authorized (*RD<sub>auth</sub>*), Refund\_Authorized (*RF<sub>auth</sub>*)}
- 2: Address [] pk // Addresses of all participants in AC<sup>2</sup>T
- 3: Mutlisignature ms // The multisigned graph  $\mathcal{D}$
- 4: State state
- 5: Header [] h // Stable block headers of block chains in  $AC^2T$
- 6: **procedure** CONSTRUCTOR(Address[] pk, MS ms( $\mathcal{D}$ ), Header[] h)
- 7: this.pk = pk
- 8: this.ms =  $ms(\mathcal{D})$
- 9: this.state = P
- 10: this.h = h
- 11: end procedure
- 12: procedure AUTHORIZEREDEEM(Evidence evd)
- 13: requires (state == P and VerifyContracts(evd))
- 14: this.state =  $RD_{auth}$  // Commit Decision
- 15: end procedure
- 16: **procedure** AUTHORIZEREFUND
- 17: requires (state == P)
- 18: this.state =  $RF_{auth}$  // Abort Decision
- $19: \ \mathbf{end} \ \mathbf{procedure}$
- 20: procedure VERIFYCONTRACTS(Evidence evd)
- 21: valid = true
- 22:  $\mathcal{D} = decrypt(ms, pk)$
- 23: for each  $e = (u, v) \in \mathcal{D}.\mathcal{E}$  do
- 24: let  $evd_e \in evd$  be e's evidence
- 25: Verify PoW and hash integrity of each block header in  $evd_e$  to ensure they follow h[e] // h[e] is the header of the stable block of e's blockchain e.BC.

26:	Let $SC_e \in evd_e$ be the smart contract of e	
27:	Verify $SC_e.s == u$ , $SC_e.r == v$ , $SC_e.a == e.a$	a
28:	Verify $SC_e.rd$ links to this smart contract stat	e
29:	Verify $SC_e.rf$ links to this smart contract stat	e
30:	Verify v's signature on $SC_e$ functions	
31:	if any verification fails then	
32:	valid = false	
33:	end if	
34:	end for	
35:	return valid	
36:	end procedure	
ι		

cuted unless all smart contracts in the  $AC^2T$  are deployed and correct and hence a commit decision can be reached.

Algorithm 3 presents a smart contract class inherited from the smart contract template in Algorithm 1 in order to use  $SC_w$ 's state as redemption and refund commitment scheme secrets. The commitment scheme is represented as a pair  $(SC_w, d)$  where  $SC_w$  is the address of the witness network coordination smart contract and d is required depth to ensure that  $SC_w$  and its state transition are stable. IsRedeemable returns true if  $SC_w$ 's state is  $RD_{auth}$  (Line 8), while IsRefundable returns true if  $SC_w$ 's state is  $RF_{auth}$ (Line 14). As the witness network is permissionless, forks could possibly happen resulting in two concurrent blocks where  $SC_w$ 's state is  $RD_{auth}$  in the first branch and  $SC_w$ 's state is  $RF_{auth}$  in the second branch. To avoid atomicity violations, participants cannot use a witness network block where  $SC_w$ 's state is  $RD_{auth}$  or  $RF_{auth}$  in their smart con-

#### Algorithm 3 Smart contract for permissionless $AC^3$ .

class PermissionlessSC extends AtomicSwapSC {

- 1: Signature  $sig_r$  // Recipient integrity signature on Smart Contract function codes.
- 2: **procedure** CONSTRUCTOR(Address r, SC  $SC_w$ , Depth d, Signature  $sig_v$ )
- 3: this.rd = this.rf =  $(SC_w, d)$
- 4: this. $sig_r = sig_v$
- 5: super(r, this.rd, this.rf) // parent constructor
- 6: end procedure
- 7: **procedure** ISREDEEMABLE(Evidence evd)
- 8: **if** evd is valid, the state of  $SC_w \in evd$  is  $RD_{auth}$ , and  $SC_w$ 's state update block is at depth  $\geq d$  **then**
- 9: return true
- 10: end if
- 11: return false
- 12: end procedure
- 13: **procedure** ISREFUNDABLE(Evidence evd)
- 14: **if** evd is valid, the state of  $SC_w \in evd$  is  $RF_{auth}$ , and  $SC_w$ 's state update block is at depth  $\geq d$  **then**
- 15: return true
- 16: end if
- 17: return false
- 18: end procedure

}

tract redemption and refund respectively unless this block is buried under at least d blocks in the witness network. As the probability of a fork at depth d (e.g., 6 blocks in the Bitcoin network [2]) is negligible,  $SC_w$ 's state eventually converges to either  $RD_{auth}$  or  $RF_{auth}$ .

The following steps summarizes the  $AC^{3}WN$  protocol steps to execute the  $AC^{2}T$  shown in Figure 1:

- 1. Alice and Bob construct the  $AC^2T$ 's graph  $\mathcal{D}$  and multisign  $(\mathcal{D}, t)$  to generate  $ms(\mathcal{D})$ .
- 2. Either Alice or Bob registers  $m_S(\mathcal{D})$  in a smart contract  $SC_w$  and publishes  $SC_w$  in the witness network setting  $SC_w$ 's state to P.  $SC_w$  follows Algorithm 2.
- 3. Afterwards, Alice publishes a smart contract  $SC_1$  using Algorithm 3 to the Bitcoin network that states the following:
  - Move X bitcoins from Alice to Bob if Bob provides evidence that  $SC_w$ 's state is  $RD_{auth}$ .
  - Refund X bitcoins from  $SC_1$  to Alice if Alice provides evidence that  $SC_w$ 's state is  $RF_{auth}$ .
  - $SC_1$  contains Bob's signature on the code of  $SC_1$ 's functions: Redeem, Refund, IsRedeemable, and IsRefundable.
- 4. Concurrently, Bob publishes a smart contract  $SC_2$  to the Ethereum network using Algorithm 3 stating the following:
  - Move Y ethers from Bob to Alice if Alice provides evidence that  $SC_w$ 's state is  $RD_{auth}$ .
  - Refund Y ethers from  $SC_2$  to Bob if Bob provides evidence that  $SC_w$ 's state is  $RF_{auth}$ .
  - $SC_2$  contains Alice's signature on the code of  $SC_2$ 's functions: Redeem, Refund, IsRedeemable, and IsRefundable.

- 5. After both  $SC_1$  and  $SC_2$  are published, any participant can submit a state change request of  $SC_w$  from Pto  $RD_{auth}$  to the witness network miners. This request is accompanied by evidence that  $SC_1$  and  $SC_2$  are published in the Bitcoin and the Ethereum blockchains respectively. The witness network miners first verify that  $SC_w$ 's state is currently P. Then, they verify that both  $SC_1$  and  $SC_2$  are published and correct in their corresponding blockchains. If these verifications succeed, the miners of the witness network record  $SC_w$ 's state change to  $RD_{auth}$  in their current block. Once a block that reflects the state change of  $SC_w$  to  $RD_{auth}$ is mined and gets buried under d blocks in the witness network, Alice and Bob can use this block as evidence to redeem their assets from  $SC_2$  and  $SC_1$  respectively.
- 6. If a participant declines to publish a smart contract, the other participant can submit a state change request of  $SC_w$  from P to  $RF_{auth}$  to the witness network miners. The witness network miners verify that  $SC_w$ 's state is currently P. If true, miners record  $SC_w$ 's state change to  $RF_{auth}$  in their current block. Once a block that reflects the state change of  $SC_w$  to  $RF_{auth}$ is mined and gets buried under d blocks in the witness network, Alice and Bob can use this block as evidence to refund their assets from  $SC_1$  and  $SC_2$  respectively.

This protocol uses two blockchain techniques to ensure that  $SC_w$ 's states  $RD_{auth}$  and  $RF_{auth}$  are mutually exclusive. First, it uses the smart contract programmable logic to ensure that  $SC_w$ 's state can only be altered from P to  $RD_{auth}$  or from P to  $RF_{auth}$ . Second, it uses the longest chain fork resolution technique to resolve forks in the witness network blockchain. This ensures that in the rare case of forking where one branch has  $SC_w$ 's state of  $RD_{auth}$  and the other branch has  $SC_w$ 's state of  $RF_{auth}$ , the fork is eventually resolved resulting in either  $SC_w$ 's state is  $RD_{auth}$  or  $SC_w$ 's state is  $RF_{auth}$  but not both.

# **5** AC<sup>3</sup>WN Analysis

This section analyzes the  $AC^3WN$  protocol introduced in Section 4.2. First, we establish that the proposed protocol ensures atomicity. Then we analyze the scalability of the witness network and how it affects the scalability of the commitment protocol. Finally, we explain how this protocol extends the functionality of previous proposals in [16, 23].

# 5.1 AC<sup>3</sup>WN: Atomicity Correctness Proof

The correctness of the AC<sup>3</sup>WN protocol depends on the stability of the underlying blockchains. For example, the stability of the Bitcoin [22] network requires that at least a majority of the mining nodes be honest and adhere to the Bitcoin's mining protocol. Also, as explained in [22], the probability of forking the Bitcoin network at depth d blocks exponentially decreases as d increases assuming the majority of mining nodes are honest. Therefore, the correctness of the AC<sup>3</sup>WN on the Bitcoin network requires the same assumptions needed for the Bitcoin network stability. First, we prove the correctness of the AC<sup>3</sup>WN protocol assuming that the witness network and the asset networks do not fork in Lemma 5.1. Then, Lemma 5.2 proves that atomicity violations are negligible in the  $AC^3WN$  protocol if the probability of forking in the witness network and the asset networks at depth d is negligible.

**Lemma 5.1.** Assume no forks in the witness network, then the  $AC^3WN$  protocol is atomic.

PROOF. Consider an AC<sup>2</sup>T executed by the AC<sup>3</sup>WN protocol and assume the atomicity of this transaction is violated. This atomicity violation implies that there exist two smart contracts  $SC_i$  and  $SC_j$  in  $AC^2T$  where  $SC_i$  is redeemed and  $SC_i$  is refunded. The redemption of  $SC_i$  implies that there exists a block in the witness network where  $SC_w$ 's state is  $RD_{auth}$  while the refund of  $SC_j$  implies that there exists a block in the witness network where  $SC_w$ 's state is  $RF_{auth}$ . Since  $SC_w$  is programmed to only allow state transitions either from P to  $RD_{auth}$  or from P to  $RF_{auth}$ , the two function calls to alter  $SC_w$ 's state from P to  $RD_{auth}$ and from P to  $RF_{auth}$  cannot take effect in one block. Miners of the witness network shall accept one and reject the other. Therefore, these two state changes must be recorded in two separate blocks. As there exist no forks in the witness network, one of these two blocks must happen before the other. This implies that either  $SC_w$ 's state is altered from  $RD_{auth}$  in one block to  $RF_{auth}$  in a following block or altered from  $RF_{auth}$  in one block to  $RD_{auth}$  in a following block. However, only state transitions from P to  $RD_{auth}$  or from P to  $RF_{auth}$  are allowed and no other state transition is permitted leading to a contradiction. 

# **Lemma 5.2.** Let the probability of forks at depth d in the permissionless witness network be negligible $< \epsilon$ , then $AC^3 WN$ protocol is atomic with a probability $> 1 - \epsilon$ .

**PROOF.** Contrapositive: assume an  $AC^2T$  executed by the AC<sup>3</sup>WN protocol and the atomicity of this transaction is violated with a probability  $p > \epsilon$ . This atomicity violation implies that there exists two smart contract  $SC_i$  and  $SC_j$  in AC<sup>2</sup>T where  $SC_i$  is redeemed and  $SC_j$  is refunded. The redemption of  $SC_i$  implies that there exists a block in the witness network where  $SC_w$ 's state is  $RD_{auth}$  while the refund of  $SC_j$  implies that there exists a block in the witness network where  $SC_w$ 's state is  $RF_{auth}$ . As  $SC_w$ 's states  $RD_{auth}$  and  $RF_{auth}$  are conflicting states, this implies that the block where  $SC_w$ 's state update to  $RD_{auth}$  occurs must exist in a fork from the block where  $SC_w$ 's state update to  $RF_{auth}$  occurs. The atomicity violation of the AC<sup>2</sup>T with a probability p implies that the fork probability in the witness network must be  $p > \epsilon$ . Hence, AC<sup>3</sup>WN is atomic with a probability  $> 1 - \epsilon$ 

# 5.2 The Scalability of AC<sup>3</sup>WN

One important aspect of  $AC^3$  protocols is *scalability*. Does using a permissionless network of witnesses to coordinate  $AC^2Ts$  limit the scalability of the  $AC^3WN$  protocol? In this section, we argue that the answer is *no*. To explain this argument, we first develop an understanding of the properties of executing  $AC^2Ts$  and the role of the witness network in executing  $AC^2Ts$ .

An  $AC^2T$  is a distributed transaction that consists of subtransactions. Each sub-transaction is executed in a

blockchain. An  $AC^3$  protocol coordinates the atomic execution of these sub-transactions across several blockchains. An  $AC^3$  protocol must ensure the atomic execution of the distributed transaction. This atomic execution of a distributed transaction requires the ACID [13, 15] execution of every sub-transaction in this distributed transaction in addition to the atomic execution of the distributed transaction itself. The ACID execution of a sub-transaction executed within a single blockchain is guaranteed by the miners of this blockchain. Miners use many techniques including mining, verification, and the miner's rationale to join the longest chain in order to implement ACID executions of transactions within a single blockchain. The atomicity of a distributed transaction is the responsibility of the distributed transaction coordinator. Therefore, the main role of the witness network in the AC<sup>3</sup>WN protocol is to ensure the atomicity of the AC<sup>2</sup>T. Since the atomicity coordination of AC<sup>2</sup>Ts is *embarrassingly parallel*, different witness networks can be used to coordinate different AC<sup>2</sup>Ts.

Assume two concurrent  $AC^2Ts$ ,  $t_1$  and  $t_2$ . The atomic execution of  $t_1$  does not require any coordination with the atomic execution of  $t_2$ . Each AC<sup>2</sup>T requires its witness network to ensure that either all sub-transactions in the AC<sup>2</sup>T are executed or none of them are. Therefore,  $t_1$  and  $t_2$  do not have to be coordinated by the same witness network.  $t_1$ can be coordinated by one witness network while  $t_2$  can be coordinated by another witness network. If  $t_1$  and  $t_2$  conflict at the sub-transaction level, this conflict is resolved by the miners of the blockchain where these sub-transactions are executed. Therefore, using a permissionless witness network to coordinate  $AC^2Ts$  does not limit the scalability of the AC<sup>3</sup>WN protocol. Different permissionless networks can be used used to coordinate different  $AC^{2}Ts$ . For example, the Bitcoin network can be used to coordinate  $t_1$  while the Ethereum network can be used to coordinate  $t_2$ .

#### 5.3 Handling Complex AC<sup>2</sup>T Graphs



Figure 4: Examples of complex graphs handled by the  $AC^{3}WN$  protocol: (a) cyclic and (b) disconnected.

One main improvement of the  $AC^3WN$  protocol over the state-of-the-art  $AC^3$  protocols in [16,23] is its ability to coordinate the atomic execution of  $AC^2Ts$  with complex graphs. This improvement is achieved because the AC<sup>3</sup>WN protocol does not depend on the rational behavior of the participants in the  $AC^2T$  to ensure atomicity. Instead, the protocol depends on a permissionless network of witnesses to coordinate the atomic execution of  $AC^2Ts$ . Once the participants agree on the AC<sup>2</sup>T graph and register it in the smart contract  $SC_w$  in the witness network, participants cannot violate atomicity as the commit and the abort decisions are decided by the state of  $SC_w$ . The state transitions of  $SC_w$  are witnessed and verified by the miners of the witness network. Therefore, the publication order of the smart contracts in the  $AC^2T$  cannot result in an advantage to any coalition among the participants. Participants can concurrently publish their smart contracts in the  $AC^2T$ , both in Figures 1 and 4, without worrying about the maliciousness of any participant.

Figure 4 illustrates two complex graph examples that either cannot be atomically executed by the protocols in [16, 23] or require additional mechanisms and protocol modifications to be atomically executed. These graphs appear in supply-chain applications. Both Nolan's and Herlihy's single leader protocol require the  $AC^2T$  graph to be acyclic once the leader node is removed. Therefore, both protocols fail to execute the transaction graph shown in Figure 4a. Removing any node from the graph in Figure 4a still results in a cyclic graph. Herlihy presents a multi-leader protocol in [16] to handle cyclic graphs. However, both Nolan's and Herlihy's protocols fail to handle disconnected graphs similar to the graph shown in Figure 4b. On the other hand, the  $AC^3WN$  protocol ensures the atomic execution of  $AC^2Ts$  irrespective of the  $AC^2T's$  graph structure.

# 6 Evaluation

This section analytically compares the performance and the overhead of the  $AC^3WN$  protocol to the state-of-the-art atomic swap protocol presented by Herilhy in [16]. First, we compare the latency of  $AC^2Ts$  as the diameter of the transaction graph  $\mathcal{D}$  increases in Section 6.1. Then, the monetary cost overhead of using a permissionless network of witnesses to coordinate a  $AC^2T$  is analyzed in Section 6.2. Afterwards, an analysis on how to choose the witness network is developed in Section 6.3. Finally, an analysis of the  $AC^2T$  throughput as the witness network is chosen from the top-4 permissionless cryptocurrencies, sorted by market cap, is presented in Section 6.4.

#### 6.1 Latency

The AC<sup>2</sup>T latency is defined as the difference between the timestamp  $t_s$  when an AC<sup>2</sup>T is started and the timestamp  $t_c$  when the AC<sup>2</sup>T is completed.  $t_s$  marks the moment when participants in the AC<sup>2</sup>T start to agree on the AC<sup>2</sup>T graph  $\mathcal{D}$ .  $t_c$  marks the completion of all the asset transfers in the AC<sup>2</sup>T by redeeming all the smart contracts in AC<sup>2</sup>T.

Let  $\Delta$  be enough time for any participant to publish a smart contract in any permissionless blockchain, or to change a smart contract state through a function call of this smart contract, and for this change to be publicly recognized [16]. Also, let  $Diam(\mathcal{D})$  be the AC<sup>2</sup>T graph diameter.  $Diam(\mathcal{D})$ is the length of the longest path from any vertex in  $\mathcal{D}$  to any other vertex in  $\mathcal{D}$  including itself.

The single leader atomic swap protocol presented in [16] has two phases: the  $AC^2T$  smart contract sequential deployment phase and the AC<sup>2</sup>T smart contract sequential redemption phase. The deployment phase requires the deployment of all smart contracts in the  $AC^{2}T$ , N, where exactly  $Diam(\mathcal{D}) \leq N$  smart contracts are sequentially deployed resulting in a latency of  $\Delta \cdot Diam(\mathcal{D})$ . Similarly, the redemption phase requires the redemption of all smart contracts in the AC<sup>2</sup>T, N, where exactly  $Diam(\mathcal{D}) < N$ smart contracts are sequentially redeemed resulting in a latency of  $\Delta \cdot Diam(\mathcal{D})$ . The overall latency of an AC<sup>2</sup>T that uses this protocol equals the latency summation of these two phases  $2 \cdot \Delta \cdot Diam(\mathcal{D})$ . Figure 5 visualizes the two phases of the protocol where time advances from left to right. As shown, some smart contracts (e.g.,  $SC_2$ ,  $SC_3$ , and  $SC_4$ ) could be deployed and redeemed in parallel but there are exactly  $Diam(\mathcal{D})$  sequentially deployed and  $Diam(\mathcal{D})$  sequentially redeemed smart contracts resulting in an overall latency of  $2 \cdot \Delta \cdot Diam(\mathcal{D})$ . Note that the protocol allows the parallel deployment and redemption of some smart contracts as long as they do not lead to an advantage to either a participant or a coalition of participants in the  $AC^{2}T$ .



Figure 5: The overall transaction latency of  $2 \cdot \Delta \cdot Diam(\mathcal{D})$  when the single leader atomic swap protocol in [16] is used.



Figure 6: The overall transaction latency of  $4 \cdot \Delta$  when the AC<sup>3</sup>WN protocol in Section 4.2 is used.

On the other hand, the  $AC^3WN$  protocol has *four* phases: the witness network smart contract deployment phase, the AC<sup>2</sup>T smart contract parallel deployment phase, the witness network smart contract state change phase, and the  $AC^{2}T$ smart contract parallel redemption phase. The witness network smart contract deployment requires the deployment of the smart contract  $SC_w$  in the witness network resulting in a latency of  $\Delta$ . The AC<sup>2</sup>T smart contract parallel deployment requires the parallel deployment of all smart contracts, N, in the AC<sup>2</sup>T resulting in a latency of  $\Delta$ . The witness network smart contract state change requires a state change in  $SC_w$  either from P to  $RD_{auth}$  or from P to  $RF_{auth}$  through  $SC_w$ 's AuthorizeRedeem or AuthorizeRefund function calls resulting in a latency of  $\Delta$ . Finally, the AC<sup>2</sup>T smart contract parallel redemption requires the parallel redemption of all smart contracts, N, in the AC<sup>2</sup>T resulting in a latency of  $\Delta$ . The overall latency of an AC<sup>2</sup>T that uses this protocol equals to the latency summation of these four phases  $4 \cdot \Delta$ . Figure 6 visualizes the four phases of the protocol where time advances from left to right. As shown, all smart contracts in the AC<sup>2</sup>T are parallelly deployed and parallelly redeemed resulting in an overall latency of  $4 \cdot \Delta$ .

Figure 7 compares the overall  $AC^2T$  latency in  $\Delta s$  resulting from Herlihy's protocol in [16] and our protocol in Section 4.2 as the transaction graph diameter,  $Diam(\mathcal{D})$  increases. As shown, our protocol achieves a constant latency of  $4 \cdot \Delta$  irrespective of the transaction diagram value while Herlihy's protocol achieves a linearly increasing latency as the transaction diameter value increases. Note that the smallest transaction graph diameter in Figure 7 starts at 2.

#### 6.2 Cost Overhead

This section analyzes the monetary cost overhead of the  $AC^3WN$  protocol in comparison to Herlihy's atomic swap protocol in [16]. As explained in Section 2, miners charge end-users a fee for every smart contract deployment and



Figure 7: The overall AC<sup>2</sup>T latency in  $\Delta s$  as the graph diameter,  $Diam(\mathcal{D})$ , increases.

every smart contract function call that results in a smart contract state change. This fee is necessary to incentivize miners to add smart contracts and append smart contract state changes to their mined blocks. As shown in Figures 5 and 6, both protocols deploy a smart contract for every edge  $e \in \mathcal{D}.\mathcal{E}$ . This results in the deployment of  $N = |\mathcal{E}|$  smart contracts in the smart contract deployment phase of both protocols. In addition, both protocols invoke a redemption or a refund function call for every deployed smart contract in the  $AC^2T$  resulting in N function calls. However, the AC<sup>3</sup>WN protocol requires the deployment of an additional smart contract  $SC_w$  in the witness network in addition to an additional function call to change  $SC_w$ 's state either from P to  $RD_{auth}$  or from P to  $RF_{auth}$ . The cost of the deployment and state transition function call of  $SC_w$  comprises the monetary cost overhead of the AC<sup>3</sup>WN protocol. Let  $f_d$ be the deployment fee of any smart contract  $SC_i \in AC^2T$ and  $f_{fc}$  be the function call fee of any smart contract function call. Then, the overall  $AC^2T$  fee of Herlihy's protocol is  $N \cdot (f_d + f_{fc})$  while the overall AC<sup>2</sup>T fee of the AC<sup>3</sup>WN protocol is  $(N+1) \cdot (f_d + f_{fc})$ . This analysis shows that  $AC^3WN$  imposes a monetary cost overhead of  $\frac{1}{N}$  the transaction fee of Herilhy's protocol assuming equal deployment and functional call fees for all the smart contracts in the  $AC^{2}T.$ 

But, how much does it cost in dollars to deploy a smart contract and make a smart contract function call? The answer is, it depends. Many factors affect a smart contract fee such as the length of the smart contract and the average transaction fee in the smart contract's blockchain [6,27]. Ryan [27] shows that the cost of deploying a smart contract with a similar logic to  $SC_w$ 's logic in the Ethereum network costs approximately \$4 when the ether to USD rate is \$300. Currently, this costs approximately \$2 assuming the current ether to USD rate of \$140.

# 6.3 Choosing the Witness Network

This section develops some insights into choosing the witness network for an  $AC^2T$ . This choice has to consider the risk of choosing different permissionless blockchain networks as the witness of an  $AC^2T$  and the relationship between this risk and the value of the assets exchanged in this  $AC^2T$ . As the state of the witness smart contract  $SC_w$  determines the state of an  $AC^2T$ , forks in the witness network present a risk to the atomicity of the  $AC^2T$ . A fork in the witness network where one block has  $SC_w$ 's state of  $RD_{auth}$  and another block has  $SC_w$ 's state of  $RF_{auth}$  might result in an atomicity violation leading to asset losses of some participants in the  $AC^{2}T$ . To overcome possible violations, our  $AC^{3}WN$  protocol does not consider a block where  $SC_{w}$ 's state is either  $RD_{auth}$  or  $RF_{auth}$  as a commit or an abort evidence until this block is buried under d blocks in the witness network. This technique of resolving forks by waiting is presented in [22] and used by Pass and Shi in [25] to eliminate uncertainty of recently mined blocks. This fork resolution technique is efficient as the probability of eliminating a fork within d blocks is sufficiently high. Waiting for d confirmations (blocks) is an essential technique to confirm the commitment of any transaction in any open blockchain that could fork. Therefore, waiting for d block confirmations is not a replacement for Herihly's and Nolan's timelocks. In fact, the timelocks of Nolan's and Herlihy's should consider waiting for d confirmations after every smart contract deployment. Recall the atomic swap example in Section 1. Alice deploys a smart contract  $SC_1$  in the Bitcoin network to transfer X bitcoins to Bob. Immediately afterwards, Bob deploys  $SC_2$  in the Ethereum network to transfer Y ethers to Alice. Now, what happens if Alice redeems the Y ethers from  $SC_2$  and the Bitcoin network gets forked before the deployment of  $SC_1$  (or the other way around). Even if timelocks are respected, this fork could result in an atomicity violation. Now, the question is whether waiting for d confirmations is sufficient to make Herlihy's protocol [16] atomic? The answer is no. Even if the smart contract deployments are buried under d blocks, the violation of timelocks due to crash failures or network denial of service at Bob could result in a refund of the bitcoins in  $SC_1$  resulting in an atomicity violation. Herlihy's protocol assumes synchrony of the network and atomicity could be violated even if there are no forks in the network.

A malicious participant in an  $AC^2T$  could fork the witness blockchain for d blocks in order to steal the assets of other participants in the  $AC^2T$ . To execute this attack, a malicious participant rents computing resources to execute a 51% attack on the witness network. The cost of an hour of 51% attack for different cryptocurrency blockchains is presented in [7]. If the cost of running this attack for d blocks is less than the expected gains from running the attack, a malicious participant is incentivized to act maliciously.

To prevent possible maliciousness, the cost of running a 51% attack on the witness network for d blocks must exceed the potential gains of running the attack. Let  $V_a$  be the value of the potentially stolen assets if the attack succeeds. Also, let  $C_h$  be the hourly cost of a 51% attack on the witness network. Finally, let  $d_h$  be the expected number of mined blocks per hour for the witness blockchain (e.g.,  $d_h = 6$  blocks / hour for Bitcoin). The value d must be set to ensure that  $V_a$  is less than the cost of running the attack for d blocks  $\frac{d \cdot C_h}{d_h}$ . Therefore d must ensure the inequality  $d > \frac{V_a \cdot d_h}{C_h}$  in order to disincentivize maliciousness. For example, let  $V_a$  be \$1M and assume Bitcoin is used for coordination. The cost per hour of a 51% attack on Bitcoin is approximately  $C_h = $300K$ . Therefore, d must be  $> \frac{\$1M \cdot 6}{\$300K} = 20$ .

# 6.4 Throughput

The throughput of the  $AC^2Ts$  is the number of transactions per second (tps) that could be processed assuming that every  $AC^2T$  spans a fixed set of blockchains and is witnessed by a fixed witness blockchain. For an  $AC^2T$  that spans multiple blockchains, the throughput is bounded by the slowest involved blockchain in the AC<sup>2</sup>T including the witness network. Let  $tps_i$  be the throughput of blockchain *i*. The throughput of the AC<sup>2</sup>Ts that span blockchains *i*, *j*, ..., *n* and are witnessed by the blockchain *w* equals  $min(tps_i, tps_j..., tps_n, tps_w)$ . Table 1 shows the throughput

Table 1: The throughput in tps of the top-4 permissionless cryptocurrencies sorted by their market cap.

Block chain	tps	Blockchain	tps
1) Bitcoin	7	3) Litecoin	56
2) Ethereum	25	4) Bitcoin Cash	61

of the top-4 permissionless cryptocurrencies sorted by their market cap [24]. An example  $AC^2T$  that exchanges assets between Ethereum and Litecoin blockchains and is witnessed by Bitcoin achieves a throughput of 7. The witness network should be chosen from the set of involved blockchains (Litecoin and Ethereum in this example) to avoid limiting transaction throughput.

### 7 Conclusion

This paper presents  $\mathrm{AC}^3\mathrm{WN},$  the first decentralized  $\mathbf{A}\mathrm{tomic}$ Cross-Chain Commitment protocol that ensures the all-ornothing atomicity semantics even in the presence of participant crash failures and network denial of service attacks. Unlike in [16,23] where the protocol correctness mainly relies on participants' rational behaviour, AC<sup>3</sup>WN separates the coordination of an Atomic Cross-Chain Transaction,  $AC^{2}T$ , from its execution. A permissionless open network of witnesses coordinates the  $AC^2T$  while participants in the  $AC^2T$ execute sub-transactions in the  $AC^2T$ . This separation allows AC<sup>3</sup>WN to ensure atomicity of all the sub-transactions in an  $AC^{2}T$  even in the presence of failures. In addition, this separation enables AC<sup>3</sup>WN to parallelly execute subtransactions in the  $AC^2T$  reducing the latency of an  $AC^2T$ from  $O(Diam(\mathcal{D}))$  in [16], where  $Diam(\mathcal{D})$  is the diameter of the AC<sup>2</sup>T graph  $\mathcal{D}$ , to O(1) irrespective of the size of the  $AC^2T$  graph  $\mathcal{D}$ . Also, this separation allows  $AC^3WN$ to scale by using different permissionless witness networks to coordinate different  $AC^2Ts$ . This ensures that using a permissionless network of witnesses for coordination does not introduce any performance bottlenecks. Finally, the AC<sup>3</sup>WN protocol extends the functionality of the protocol in [16] by supporting  $AC^2Ts$  with complex graphs (e.g., cyclic and disconnected graphs). AC<sup>3</sup>WN introduces a slight monetary cost overhead to the participants in the  $AC^{2}T$ . This cost equals the cost of deploying a coordination smart contract in the witness network plus the cost of a function call to the coordination smart contract to decide whether to commit or to abort the  $AC^{2}T$ . The smart contract deployment and function call approximately cost \$2 combined per  $AC^{2}T$  when Ethereum is used to coordinate the  $AC^{2}T$ .

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# 9 References

- Atomic cross-chain trading. https://en.bitcoin.it/ wiki/Atomic\_cross-chain\_trading, 2018.
- [2] Bitcoin confirmations. https: //www.buybitcoinworldwide.com/confirmations/, 2018.
- [3] Coinbase. https://coinbase.com, 2018.
- [4] Robinhood. https://robinhood.com/, 2018.
- [5] Solidity solidity 0.5.5 documentation. https://solidity.readthedocs.io/en/v0.5.5/, 2018.
- [6] Avg. transaction fee historical chart. https://bitinfocharts.com/comparison/ transactionfees-btc-eth.html, 2019.
- [7] Cost of a 51% attack for different cryptocurrencies. https://www.crypto51.app/, 2019.
- [8] P. A. Bernstein, V. Hadzilacos, and N. Goodman. Concurrency control and recovery in database systems. 1987.
- [9] V. Buterin et al. A next-generation smart contract and decentralized application platform. *white paper*, 2014.
- T. Dickerson, P. Gazzillo, M. Herlihy, and E. Koskinen. Adding concurrency to smart contracts. In Proceedings of the ACM Symposium on Principles of Distributed Computing, pages 303–312. ACM, 2017.
- [11] I. Eyal, A. E. Gencer, E. G. Sirer, and R. Van Renesse. Bitcoin-ng: A scalable blockchain protocol. In NSDI, pages 45–59, 2016.
- [12] O. Goldreich. Foundations of cryptography: volume 1, basic tools. Cambridge University Press, Cambridge, 2001.
- [13] J. Gray et al. The transaction concept: Virtues and limitations. In VLDB, volume 81, pages 144–154. Citeseer, 1981.
- [14] J. N. Gray. Notes on data base operating systems. In Operating Systems, pages 393–481. Springer, 1978.
- [15] T. Haerder and A. Reuter. Principles of transaction-oriented database recovery. ACM computing surveys (CSUR), 15(4):287–317, 1983.
- [16] M. Herlihy. Atomic cross-chain swaps. In Proceedings of the 2018 ACM symposium on principles of distributed computing, pages 245–254, 2018.

- [17] M. Herlihy. Blockchains from a distributed computing perspective. Communications of the ACM, 62(2):78–85, 2019.
- [18] E. K. Kogias, P. Jovanovic, N. Gailly, I. Khoffi, L. Gasser, and B. Ford. Enhancing bitcoin security and performance with strong consistency via collective signing. In 25th USENIX Security Symposium (USENIX Security 16), pages 279–296, 2016.
- [19] L. Luu, V. Narayanan, C. Zheng, K. Baweja, S. Gilbert, and P. Saxena. A secure sharding protocol for open blockchains. In *Proceedings of the 2016 ACM SIGSAC Conference on Computer and Communications Security*, pages 17–30. ACM, 2016.
- [20] S. Maiyya, V. Zakhary, D. Agrawal, and A. E. Abbadi. Database and distributed computing fundamentals for scalable, fault-tolerant, and consistent maintenance of blockchains. *PVLDB*, 11(12):2098–2101, 2018.
- [21] S. Micali. Algorand: the efficient and democratic ledger. CoRR, abs/1607.01341, 2016.
- [22] S. Nakamoto. Bitcoin: A peer-to-peer electronic cash system. 2008.
- [23] T. Nolan. Alt chains and atomic transfers. https://bitcointalk.org/index.php?topic= 193281.msg2224949#msg2224949, 2013.
- [24] D. O'Keeffe. Understanding cryptocurrency transaction speeds. https://medium.com/coinmonks/ understanding-cryptocurrency-transactionspeeds-f9731fd93cb3, 2018.
- [25] R. Pass and E. Shi. Hybrid consensus: Efficient consensus in the permissionless model. In 31st International Symposium on Distributed Computing (DISC 2017). Schloss Dagstuhl-Leibniz-Zentrum fuer Informatik, 2017.
- [26] R. L. Rivest, A. Shamir, and L. Adleman. A method for obtaining digital signatures and public-key cryptosystems. *Communications of the ACM*, 21(2):120–126, 1978.
- [27] D. Ryan. Costs of a real world ethereum contract. https://hackernoon.com/costs-of-a-real-worldethereum-contract-2033511b3214, 2017.
- [28] G. Wood. Ethereum: A secure decentralised generalised transaction ledger. *Ethereum project* yellow paper, 151:1–32, 2014.